

Measuring Confounder Influence

MILO SCHIELD

Augsburg College Department of Business Administration
Director, W. M. Keck Statistical Literacy Project

THOMAS V.V. BURNHAM

Cognitive Consulting

9 August 2004

www.augsburg.edu/ppages/~schield

schield@augburg.edu

Meaning of an Association

An association obtained from statistics in a random sample can be:

“Statistically significant” if very unlikely when due solely to the influence of chance.

“Confounder resistant” if strongly resistant to nullification by a large confounder

Quantitative measures are needed to be useful!

“Resistance”

Rules of Thumb

Sir Richard Doll: No single study is persuasive unless the lower limit of its 95% confidence level falls above a **threefold** increased risk.

“As a general rule of thumb,” says Angell of the New England Journal, “we are looking for a relative risk of **three or more**” before accepting a paper.

Robert Temple, FDA Director of Drug Evaluation, puts it bluntly: "My basic rule is if the relative risk isn't at least **three or four**, forget it."

Problem of Confounding in Epidemiology

John Bailar, epidemiologist: *“There is no reliable way of identifying the dividing line.”*

Epidemiologists need an abstract description of confounding that can generate confounder significance and confounder intervals for RR.

This description must handle binary data, be meaningful, useful and easy to understand.

“S Confounder”

Confounder Resistant

A is predictor, B is confounder, E is effect.

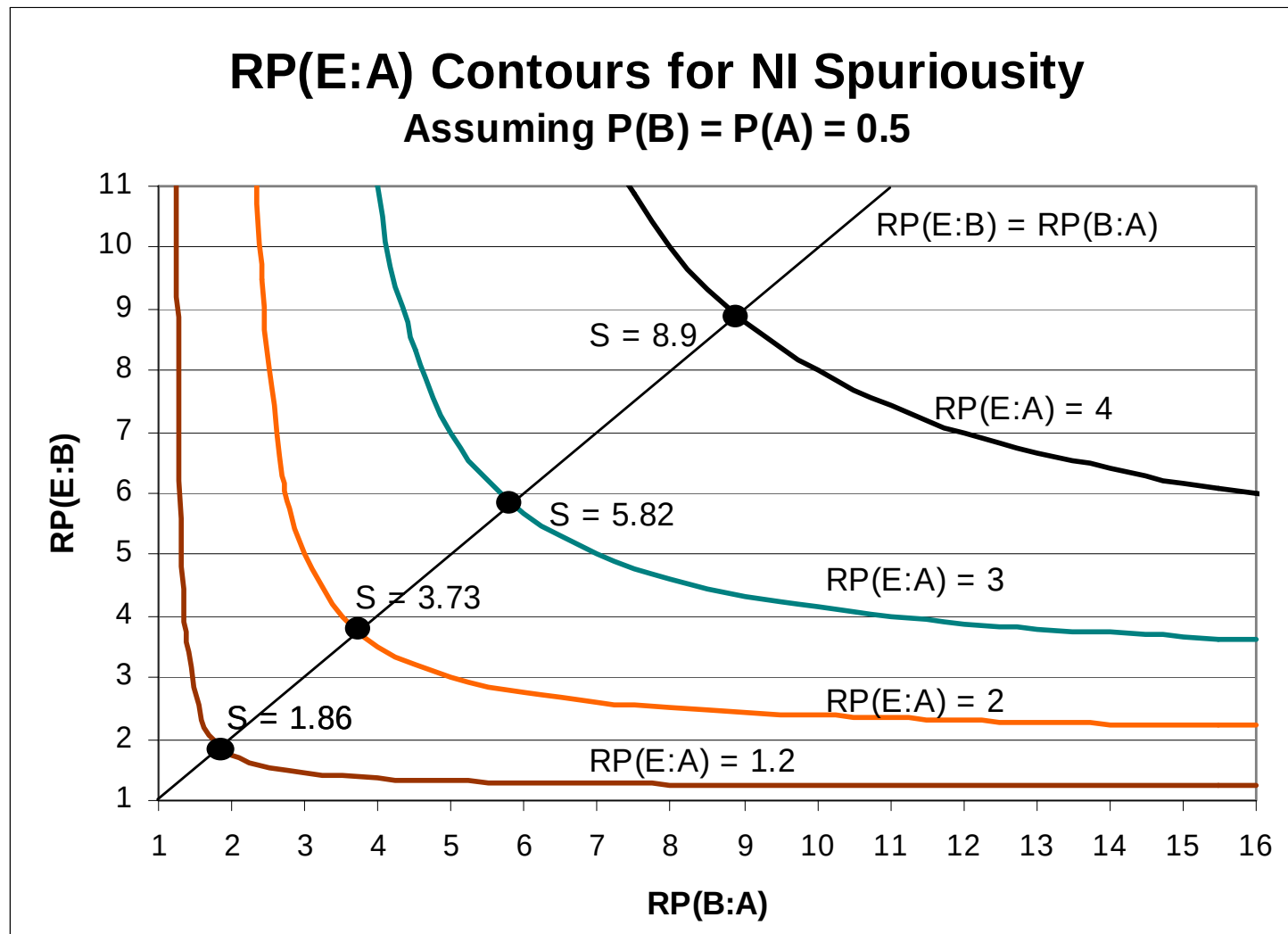
- * $P(B)$ = Prevalence of the confounder.
 $P(A)$ = Prevalence of predictor.
- * $RP(E:B)$ = Rel. Prev of effect for confounder
- * $RP(B:A)$ = Rel, Prev of confounder for predictor.

An **S confounder** is a binary confounder where
 $RP(B:A) = RP(E:B) = S$ and $P(B) = P(A)$.

An association is “**confounder resistant**” to a size S confounder if it withstands nullification.

Spuriousity Contours

Schield & Burnham (2003)



Algebraic Condition to Resist Nullification

The confounder size, S , and predictor prevalence, $P(A)$, determine the minimum excess relative risk, $XRP(E:A)$, that can resist nullification.

1.

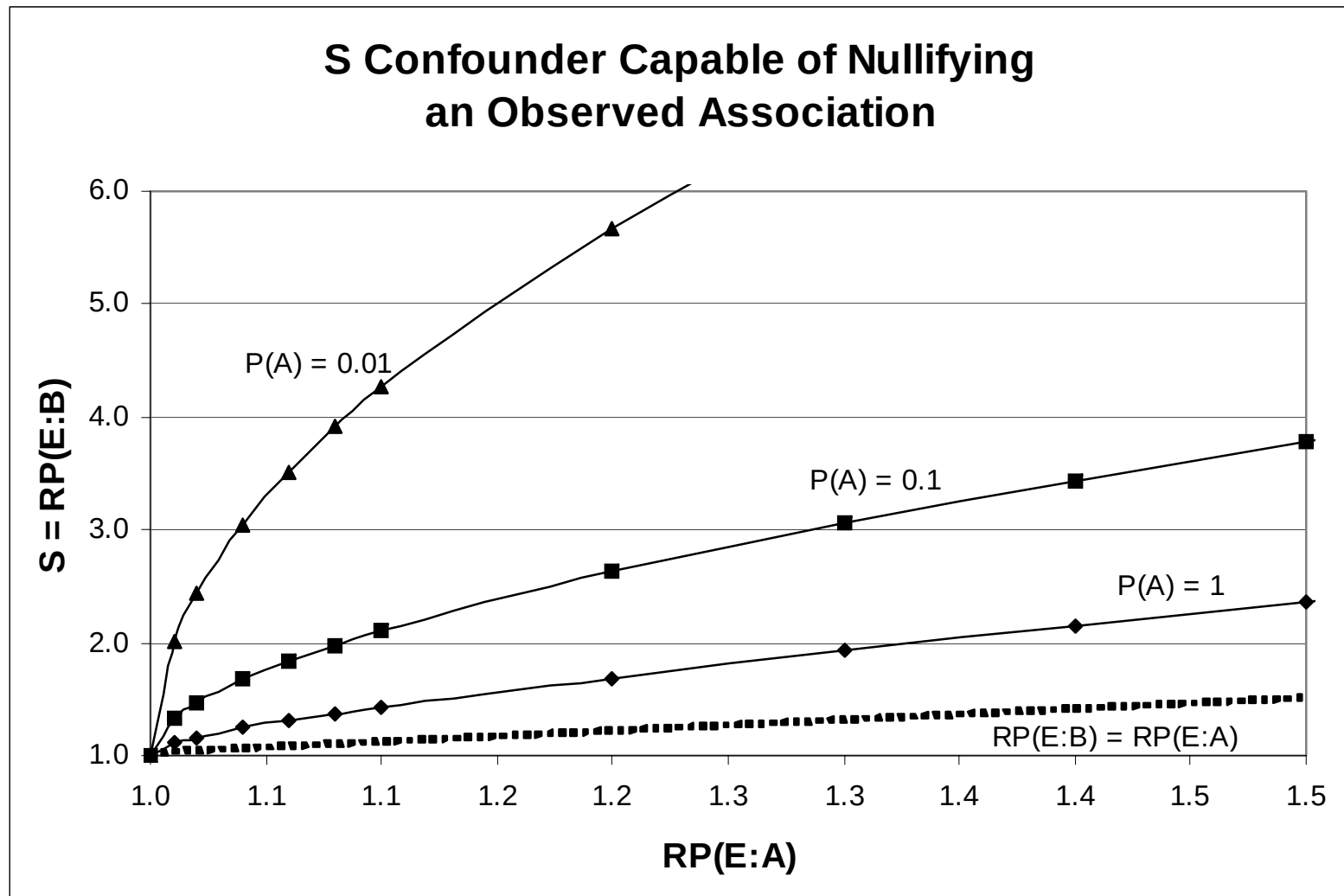
$$XRP(E : A) = P(A) \cdot (S - 1)^2 / \{1 + [2P(A) \cdot (S - 1)]\}$$

If the predictor prevalence is 50%, then

$$XRP(E : A) = (S - 1)^2 / (2S)$$

If $S = 5$, $RP(E:A) = 2.6$; if $S = 6$, $RP(E:A) = 3.1$

Confounder Size Needed to Nullify a Relative Risk



Confounder Intervals: Influence of Confounder

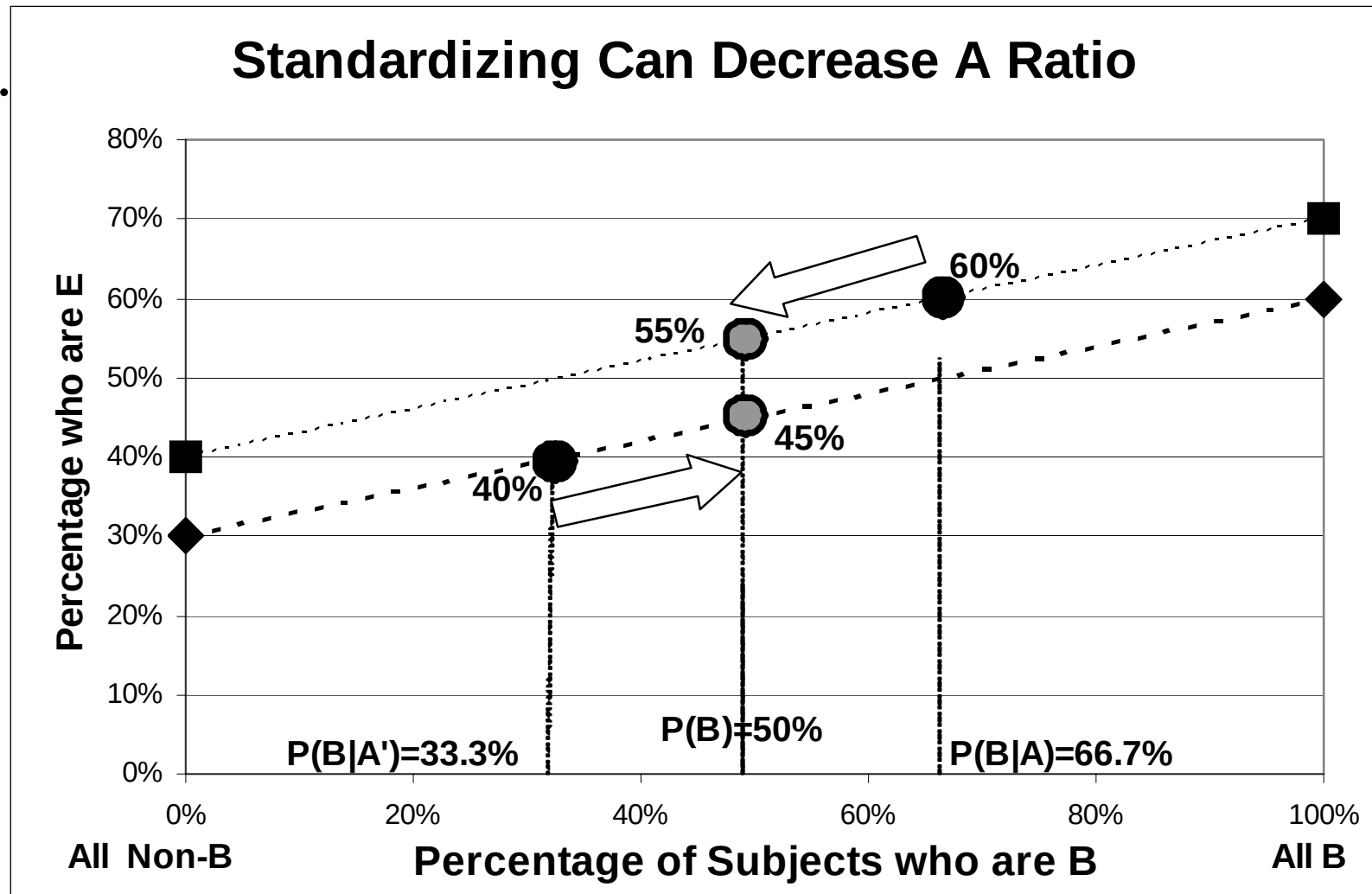
Lower limit: determined by removing the influence of a confounder where $RP(B:A) = RP(E:B)$.

Upper limit: determined by removing the influence of a confounder where $RP(B:A) = 1/RP(E:B) = 1/S$.

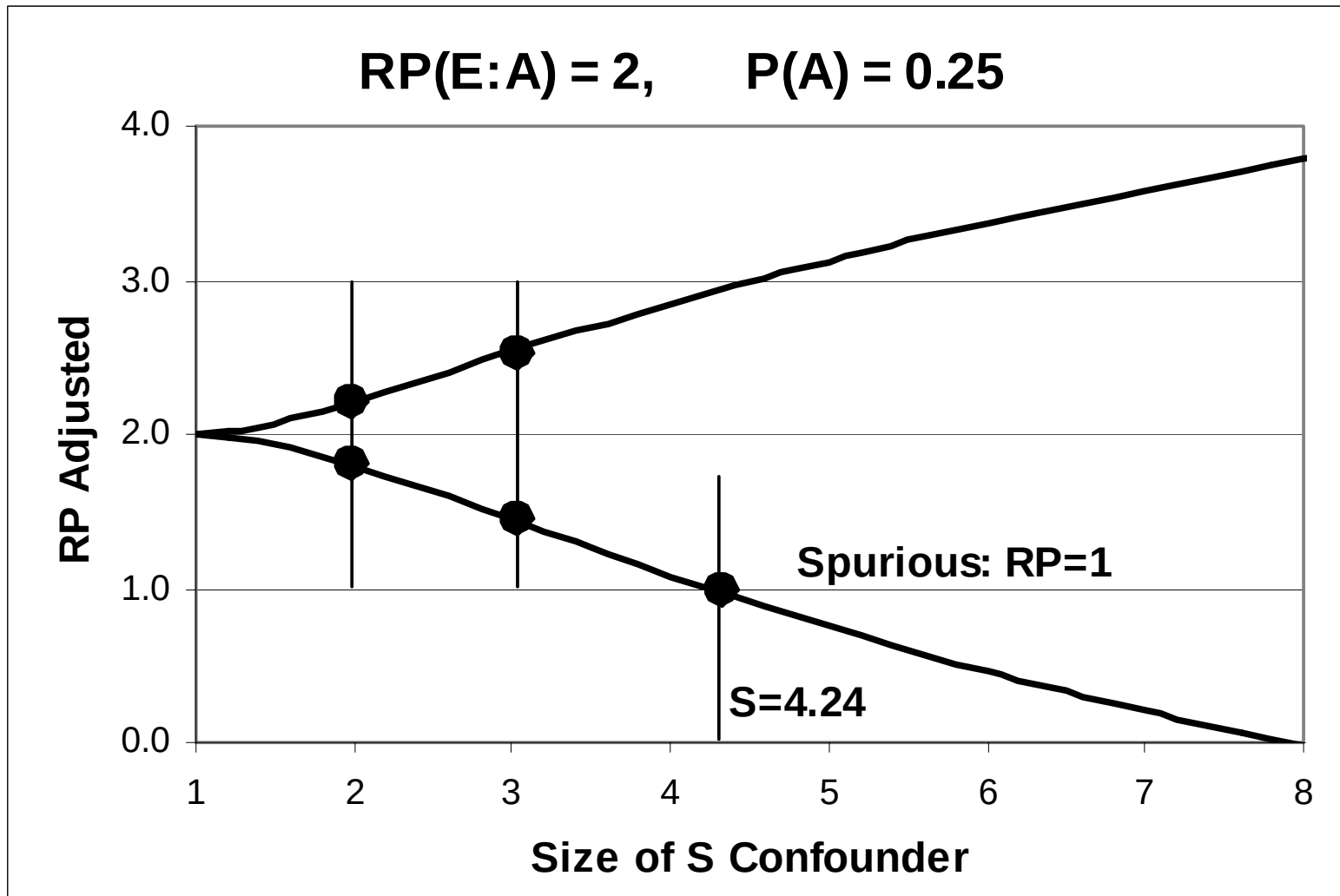
Given the size of an S confounder, the confounder influence can be determined algebraically and illustrated using a standardization diagram.

For a S confounder of size 2, the confounder interval for $RP(E:A) = 2$ with $P(A) = 0.5$ is $[1.67, 3.0]$.

Standardizing Shows Influence of Confounder



Confounder Intervals





Recommendations

Statistical educators should find ways to teach confounder influence in the first course.

Analysts should show confounder susceptibility: either give confounder intervals or identify the S confounder needed to nullify an association.

Subject experts should set generally accepted confounder sizes for confounder resistance: e.g., $S = 6$ for $P(A) = 50\%$.